



CHRISTIAN-ALBRECHTS-UNIVERSITÄT ZU KIEL

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Aufgaben zur Vorlesung »Approximative Algorithmen«

Blatt 1

Hausaufgabe 1.1 (MAX-SAT (6 Points))

Give a prove for the omitted claims from the randomized algorithm for the MAX-SAT problem:

1. Show that for all $k \geq 1$:

$$1 - \left(1 - \frac{1}{k}\right)^k \geq 1 - \frac{1}{e}.$$

Hint: Use that $(1 + \frac{1}{n})^n$ is monotone in n and $e = \lim_{n \rightarrow \infty} (1 + \frac{1}{n})^n$.

2. Show that for all $z \in [0, 1]$ and $k \in \mathbb{N}^+$:

$$1 - \left(1 - \frac{z}{k}\right)^k \geq \left(1 - \left(1 - \frac{1}{k}\right)^k\right)z.$$

Hint: Prove that $f : [0, 1] \rightarrow \mathbb{R}, z \mapsto 1 - \left(1 - \frac{z}{k}\right)^k$ is concave.

3. Show that for every k positive numbers a_1, \dots, a_k :

$$\frac{1}{k} \sum_{i=1}^k a_i \geq \left(\prod_{i=1}^k a_i \right)^{1/k}.$$

Hausaufgabe 1.2 (MAX-SAT (4 Points))

Determine for each $k \in \{1, 2, 3, 4\}$ which method (1 or 2) will give the better results, if each clause contains exactly k literals.